

# THE KICKER THEOREM

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PREFERENCE AGGREGATION IN MULTIAGENT SYSTEMS

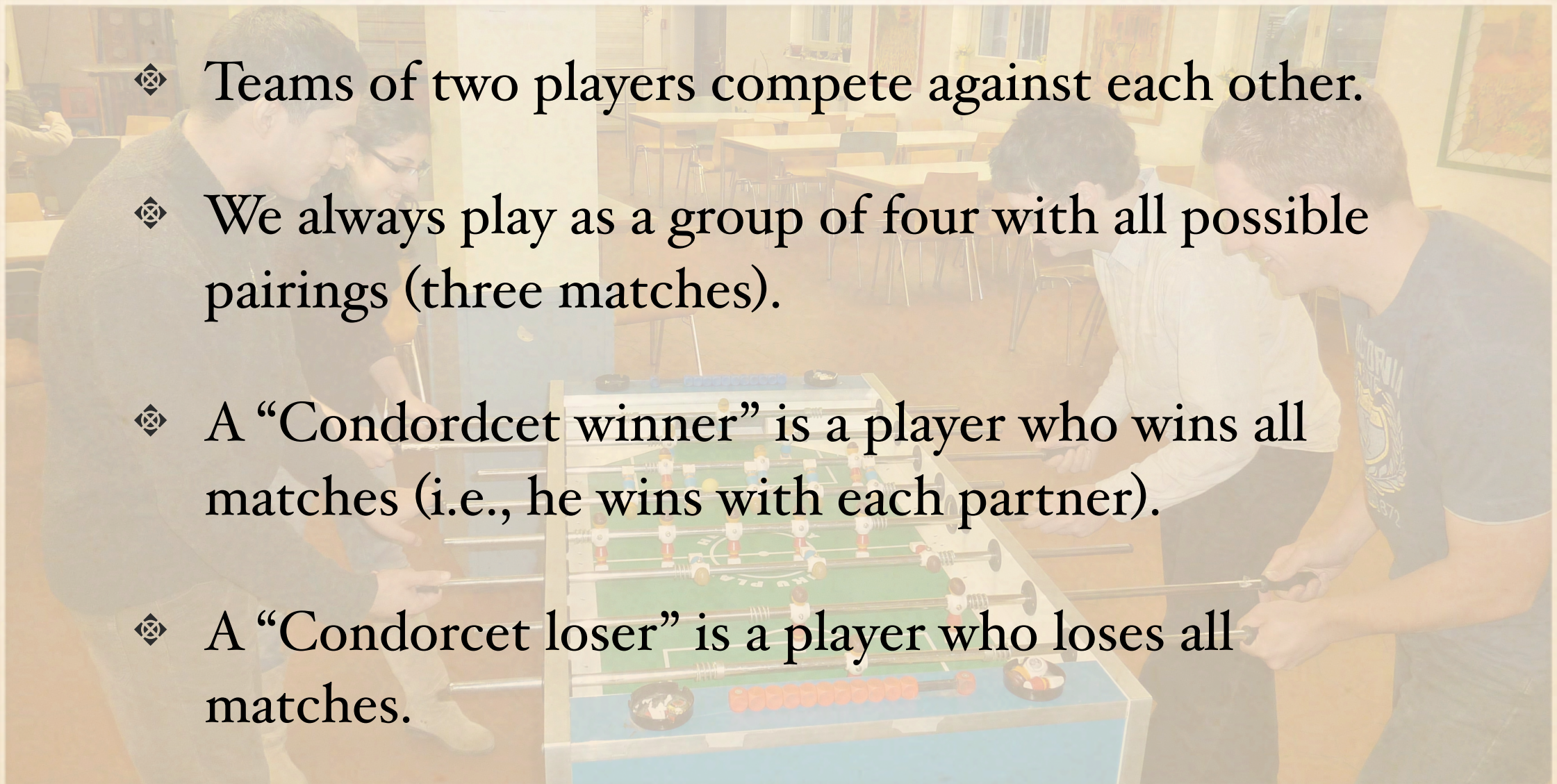


# PRELIMINARIES

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KICKER (🇩🇪) ♣️ FOOSBALL (🇬🇧)

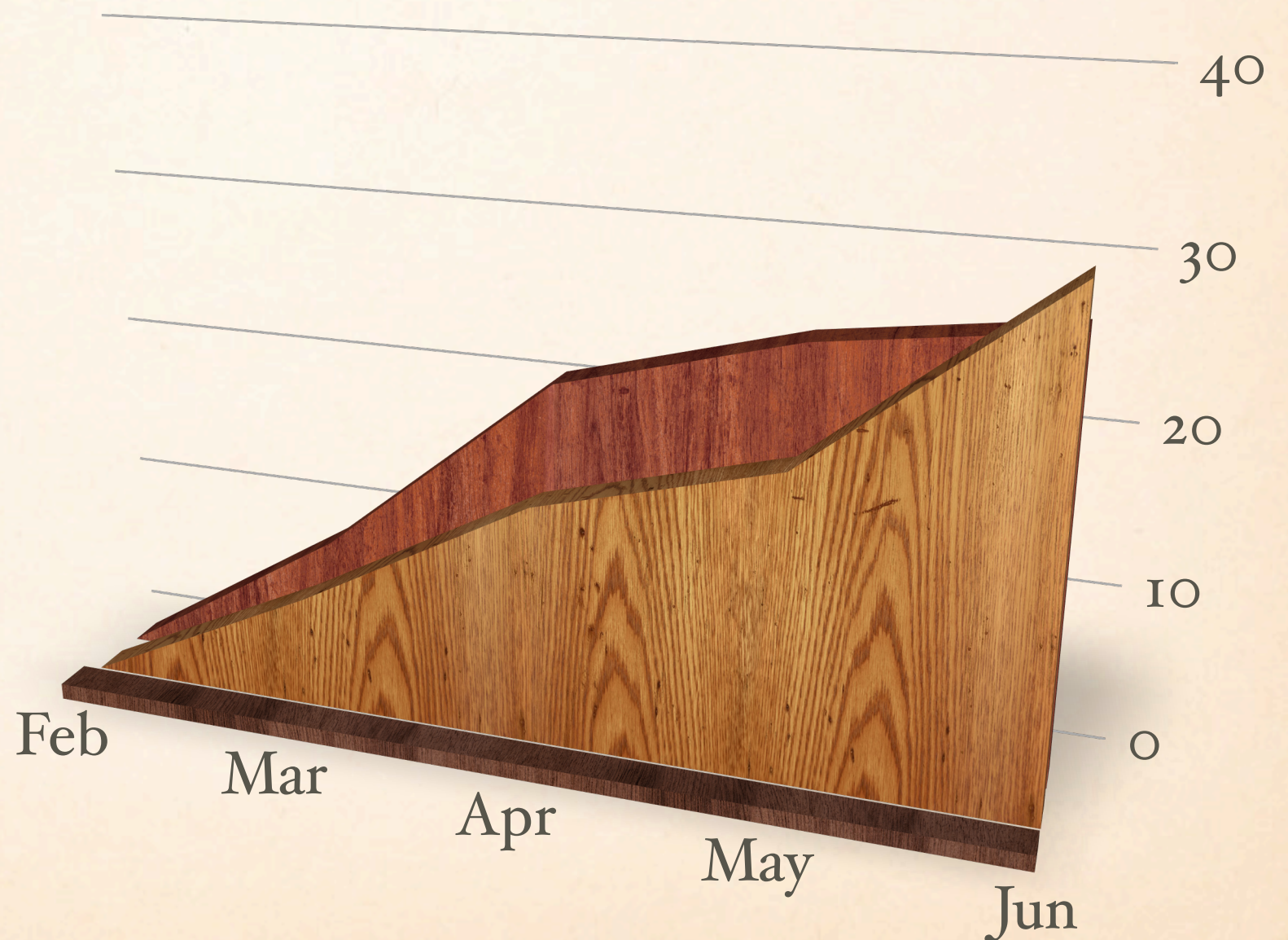
- ❖ Teams of two players compete against each other.
- ❖ We always play as a group of four with all possible pairings (three matches).
- ❖ A “Condorcet winner” is a player who wins all matches (i.e., he wins with each partner).
- ❖ A “Condorcet loser” is a player who loses all matches.





# EXPERIMENTAL DATA

- none
- Condorcet winner
- Condorcet loser





# ANALYTIC INVESTIGATION

❖ **Conjecture** (Fischer, 2007): Every Kicker Tournament either admits a Condorcet winner or a Condorcet loser.

❖ **Proof** (Harrenstein, about 5 minutes later):

$$ab > cd$$

wlog  $ac > bd$

Case 1:  $ad > bc$  ( $\Rightarrow$  a is Condorcet winner)


Case 2:  $ad < bc$  ( $\Rightarrow$  d is Condorcet loser) □

❖ The potential Condorcet winner (a) and the potential Condorcet loser (d) always play together in the last match.

❖ **Corollary:** It also works for Tennis doubles and Bridge!



# IMPACT



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**Navigation**

[Home](#)

[Open problems](#)

[Journal versions](#)

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[Mensa, Lawi, LfF](#)

[LVG \(Mischel\)](#)

[AGT Blog](#)

[Complexity Blog](#)

[Haris' Blog](#)

[Shtetl-Optimized](#)

[OR Blog](#)

**Home**

Current research

- Retentiveness
- Coalition formation games
- Convergence of fictitious play
- Dominance-based solution concepts
- Generalizing tournament solutions to incomplete tournaments
- what else?

Upcoming conferences/workshops:

- [STACS 2010](#), Nancy, March 4-6, 2010
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- [AAAI 2010](#), Atlanta, July 11-15, 2010
- [EURO XXIV](#), Lisbon, July 11-14, 2010
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- [Second Brazilian Workshop of the Game Theory Society](#), São Paulo, July 29-August 4, 2010
- [Int. Conf. Operations Research](#), Munich, September 1-3, 2010
- [COMSOC 2010](#), Düsseldorf, September 13-16, 2010
- [SAGT 2010](#), Athens, October 18-20, 2010
- [FOCS](#), Las Vegas, October 23-26, 2010

**61**

days until



**SAGT deadline**

**73**

days until

**COMSOC deadline**

**Reigning Condorcet Winner**

[History](#)

**60**

days until


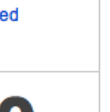
**SAGT deadline**

**72**

days until

**COMSOC deadline**

**Submitting Condorcet Loser**





**Attachments (1)**

[pamas\\_guide.pdf](#) - on Nov 4, 2009 2:07 PM by Felix Brandt (version 2 / [earlier versions](#)) [Remove](#)

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[Home](#)

[Open problems](#)

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**PAMAS**

**Thursday, March 4**

[Print](#)

- Friday, March 5**
- [AAAI reviews](#)
- [Weißwurstfrühstück](#)
- Sunday, March 7**
- [Dagstuhl Seminar](#)
- Monday, March 8**
- [Dagstuhl Seminar](#)
- [AAAI author feedback](#)
- Tuesday, March 9**
- [Dagstuhl Seminar](#)
- [AAAI author feedback](#)
- [HG: GraduateSchool-Kickoff](#)
- Wednesday, March 10**
- [Dagstuhl Seminar](#)
- [AAAI author feedback](#)
- [HG: GraduateSchool-Kickoff](#)
- [AAAI response](#)
- Thursday, March 11**
- [Dagstuhl Seminar](#)
- [HG: GraduateSchool-Kickoff](#)
- [AAAI response](#)
- Friday, March 12**
- [Dagstuhl Seminar](#)
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- [AAAI response](#)

Events shown in time zone: Berlin [Google Calendar](#)



# OPEN PROBLEM

- ❖ We were unable to generalize this in any meaningful sense, e.g.,
- ❖ more players,
- ❖ more players per team,
- ❖ matches of more than two teams, etc.

